

39. (a) Let  $F_A$  and  $F_B$  be the forces exerted by the wires on the log and let  $m$  be the mass of the log. Since the log is in equilibrium  $F_A + F_B - mg = 0$ . Information given about the stretching of the wires allows us to find a relationship between  $F_A$  and  $F_B$ . If wire  $A$  originally had a length  $L_A$  and stretches by  $\Delta L_A$ , then  $\Delta L_A = F_A L_A / AE$ , where  $A$  is the cross-sectional area of the wire and  $E$  is Young's modulus for steel ( $200 \times 10^9 \text{ N/m}^2$ ). Similarly,  $\Delta L_B = F_B L_B / AE$ . If  $\ell$  is the amount by which  $B$  was originally longer than  $A$  then, since they have the same length after the log is attached,  $\Delta L_A = \Delta L_B + \ell$ . This means

$$\frac{F_A L_A}{AE} = \frac{F_B L_B}{AE} + \ell .$$

We solve for  $F_B$ :

$$F_B = \frac{F_A L_A}{L_B} - \frac{AE\ell}{L_B} .$$

We substitute into  $F_A + F_B - mg = 0$  and obtain

$$F_A = \frac{mgL_B + AE\ell}{L_A + L_B} .$$

The cross-sectional area of a wire is  $A = \pi r^2 = \pi(1.20 \times 10^{-3} \text{ m})^2 = 4.52 \times 10^{-6} \text{ m}^2$ . Both  $L_A$  and  $L_B$  may be taken to be 2.50 m without loss of significance. Thus

$$\begin{aligned} F_A &= \frac{(103 \text{ kg})(9.8 \text{ m/s}^2)(2.50 \text{ m}) + (4.52 \times 10^{-6} \text{ m}^2)(200 \times 10^9 \text{ N/m}^2)(2.0 \times 10^{-3} \text{ m})}{2.50 \text{ m} + 2.50 \text{ m}} \\ &= 866 \text{ N} . \end{aligned}$$

- (b) From the condition  $F_A + F_B - mg = 0$ , we obtain

$$F_B = mg - F_A = (103 \text{ kg})(9.8 \text{ m/s}^2) - 866 \text{ N} = 143 \text{ N} .$$

- (c) The net torque must also vanish. We place the origin on the surface of the log at a point directly above the center of mass. The force of gravity does not exert a torque about this point. Then, the torque equation becomes  $F_A d_A - F_B d_B = 0$ , which leads to

$$\frac{d_A}{d_B} = \frac{F_B}{F_A} = \frac{143 \text{ N}}{866 \text{ N}} = 0.165 .$$